

# A Peculiar Linearly Cover Variant of Amensalsim in Mathematical Ecology with Restricted Resources: Case(IV)

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## Abstract

*The structure of this model is made up of two nonlinear differential equations of the first order. They are both standing in for the Amensal and the Enemy Species. The effects of decline rate of enemy species due to natural restrictions on the formed model are analysed and discussed in this paper. The Amensal Species has restricted resources and a cover defence that varies linearly, providing them with some measure of safety from the assaults of enemy species. When further investigation is carried out, the necessary graphs have been illustrated with it so that the nature of the relationship with interactions between the two species can be observed more closely.*

## 1.Introduction:

K.V.L.N.Acharyulu and N.Ch.Pattabhi Ramacharyulu explored the local and global stabilities of an Ammensal-enemy ecological model by forming quasi-linear basic equations [2-9]. In past research, An Ammensal-enemy eco-system with varied resources was analysed for stability under various situations. Some scholars, such as, pioneered new eras [1,10-18] by establishing efficient ways for resolving a number of obstacles when investigating species interactions. This study's main goal is to examine how the two species interact owing to enemy species' natural decrease rate.

**2. Basic Equations of the Considered Model:**

A strange linearly cover variant of Amensalism with Limited Resources in Mathematical Ecology are considered as

$$dX/dt = aX - bX^2 - c(X - (d + eX))Y$$

$$dY/dt = fY - gY^2$$

Here x and y stand for Amensal and Enemy growth rates respectively. The natural growth rates of Amensal and enemy species are referred as a and f. c is the Amensal coefficient.

b and g are the two species' decline rates due to natural resource restrictions. d+ex is the Amensal population, which protected from the attacks of enemy species by maintaining constant values for d and e.

**3. Case(i): The influence of g on Amensal-Enemy Model**

For investigating the interaction between Amensal and Enemy Species, the following values of concerned parameters are considered.

**Table(1)**

a	b	c	d	e	f	g	X <sub>0</sub>	Y <sub>0</sub>
1.1100	0.889	2.515	0.875	0.67	0.859	changes	0.134	0.366

The impact of changing the parameter g on the model in view of possible Dominance time instincts .

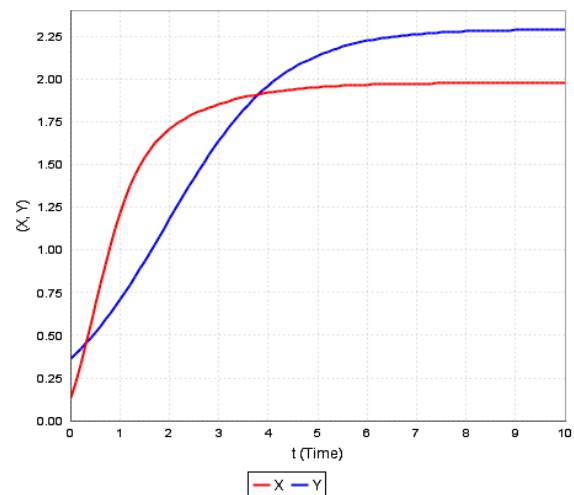
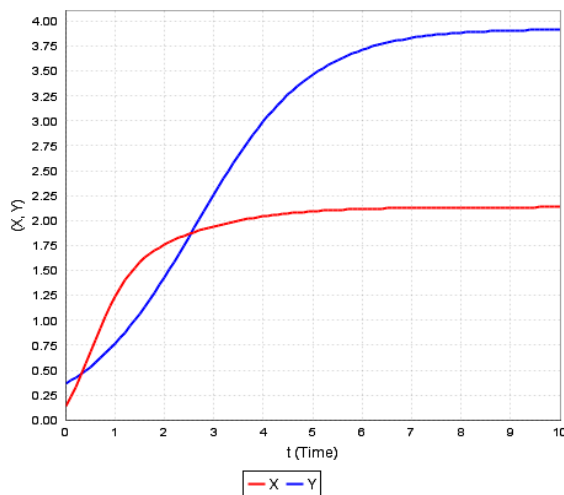
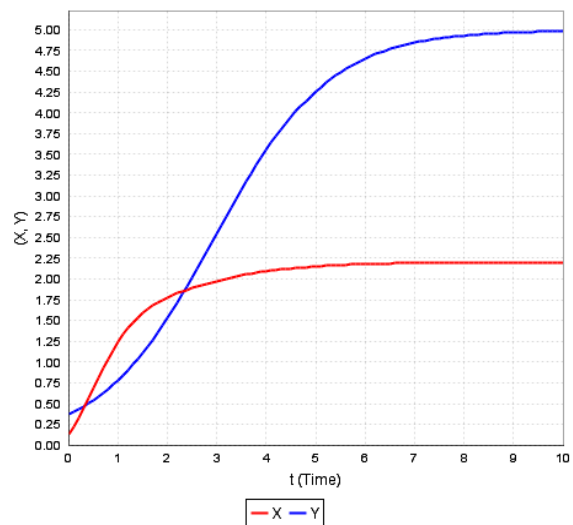
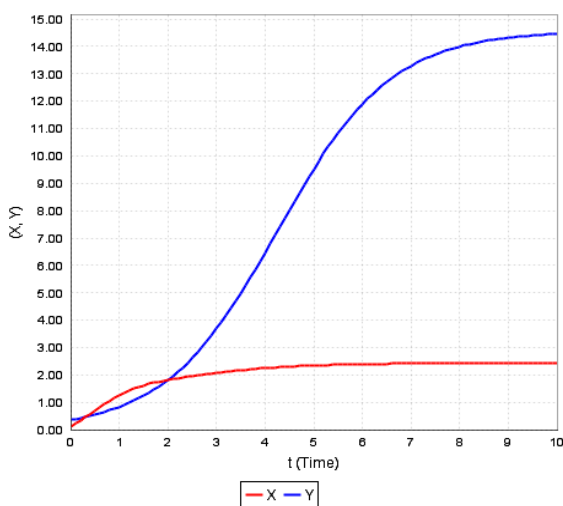
**Table(2)**

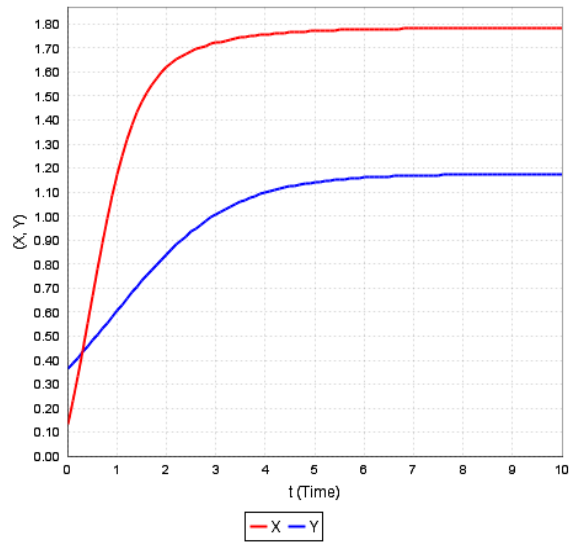
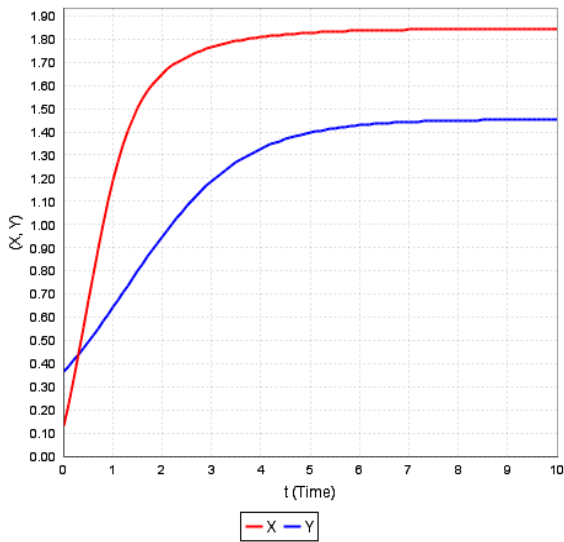
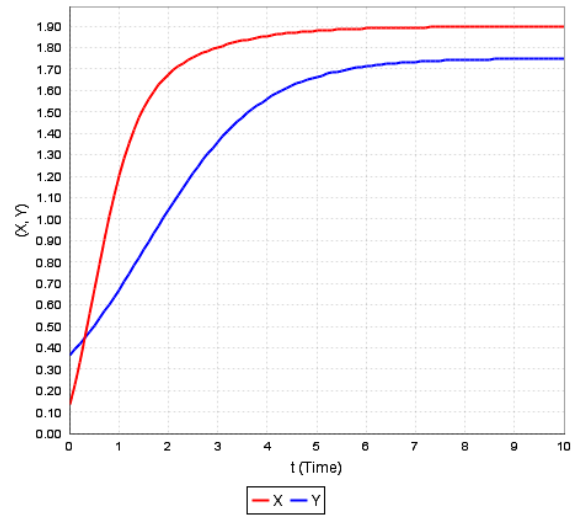
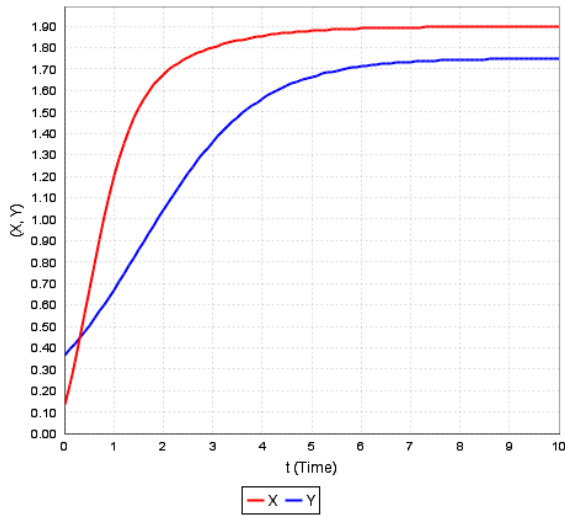
S.NO	g	t <sub>1</sub> <sup>*</sup>	t <sub>2</sub> <sup>*</sup>
1	0.0590	0.375	2
2	0.1720	0.37	2.75
3	0.2190	0.365	2.60
4	0.3750	0.36	3.85

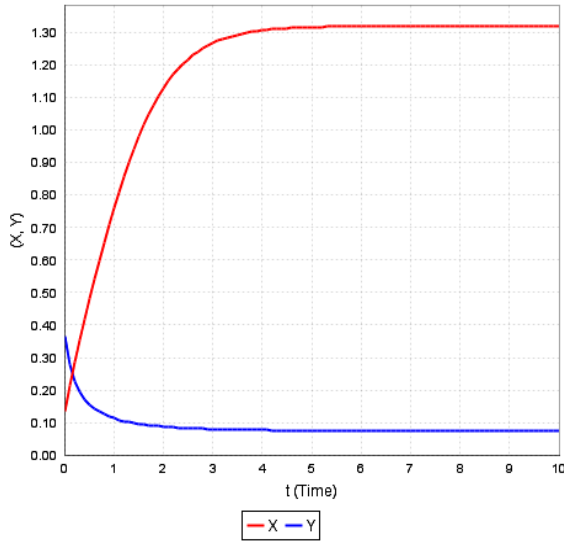
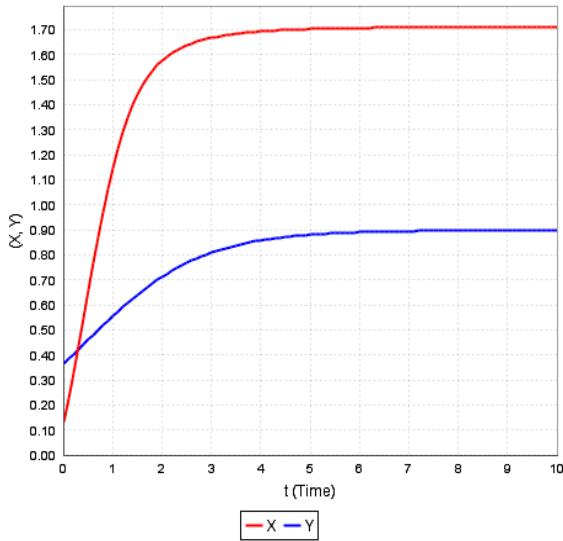
5	0.4910	0.32	*
6	0.5910	0.3	*
7	0.7310	0.295	*
8	0.8160	0.29	*
9	0.9560	0.28	*

Fig(1) to Fig(10): when  $a=1.1100, b=0.889, c=2.515, d=0.875, e=0.67, f=0.859, X_0=0.134, Y_0=0.366$

Vs change in g







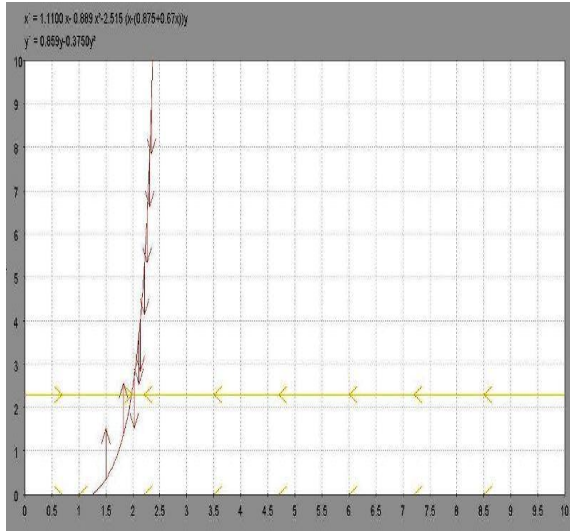
**4. Conclusions:** The change of Ammensal growth rate significantly influences on the Ammensal-Enemy Species. Initially Ammensal Species is dominated by Enemy Species, in a course time Ammensal dominates enemy species. Meanwhile dominance reversal time occurred two times at  $t_1^*$  and  $t_2^*$ . Here  $t_1^*$  gradually decreases and  $t_2^*$  Gradually increases.

**5. Phase Plane Analysis:**

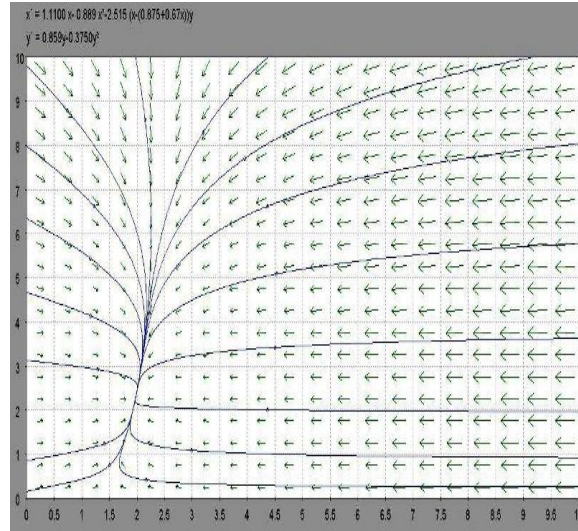
Phase plane analysis has been carried out to analyze the model for establishing stability with equilibrium points which are associated with Eigen values.

When  $a=0.375, b=0.889, c=2.515, d=0.875, e=0.67, f=0.859, g=0.5$

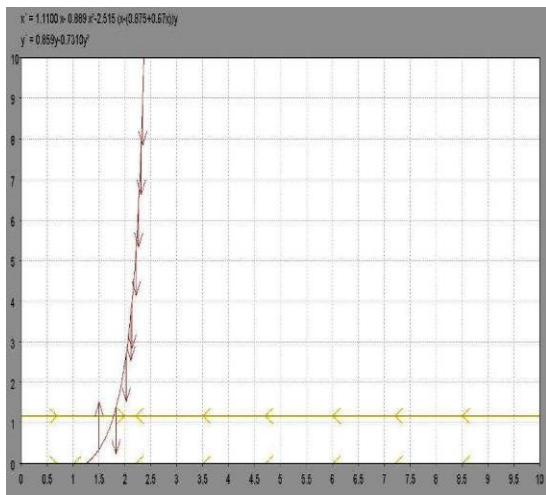
S.No	Values of Parameter(g)	Equilibrium Point	Jacobian matrix	Eigenvalues	eigenvectors
1	0.3750	(1.9775, 2.2907)	$\begin{bmatrix} -4.3071 & 0.5594 \\ 0 & -0.859 \end{bmatrix}$	$\lambda_1 = -0.859$ $\lambda_2 = -4.3071$	$E_1 = (0.1601, 0.9870)^T$ $E_2 = (0, 1)^T$
2	0.7310	(1.783, 1.1751)	$\begin{bmatrix} -3.0354 & 0.72083 \\ 0 & -0.859 \end{bmatrix}$	$\lambda_1 = -0.859$ $\lambda_2 = -3.0354$	$E_1 = (0.3144, 0.9492)^T$ $E_2 = (0, 1)^T$
3	0.9560	(1.710, 0.8985)	$\begin{bmatrix} -2.676 & 0.7811 \\ 0 & -0.859 \end{bmatrix}$	$\lambda_1 = -0.859$ $\lambda_2 = -2.676$	$E_1 = (0.3948, 0.9187)^T$ $E_2 = (0, 1)^T$



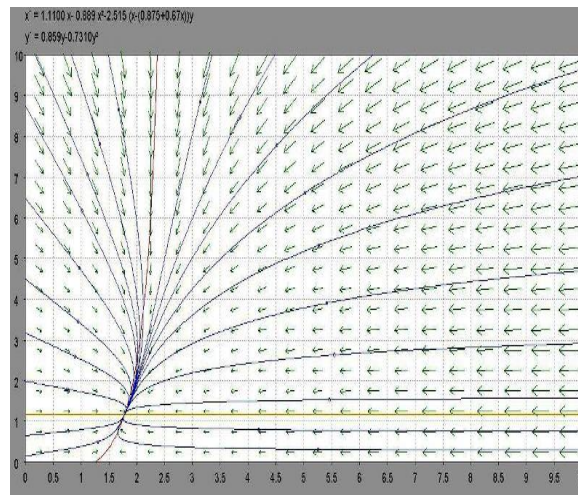
Phase Plane Figure(1)



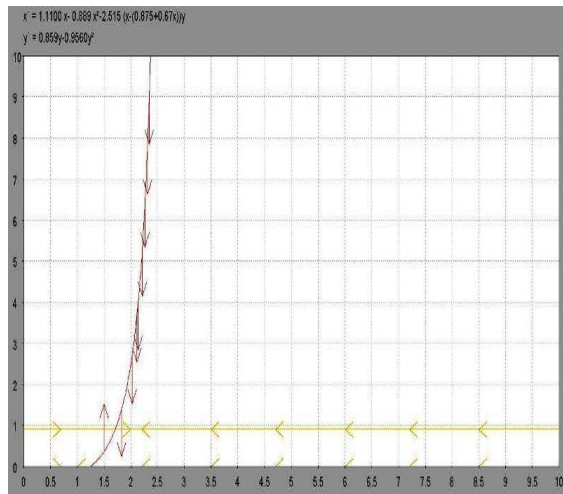
Phase Plane Figure(2)



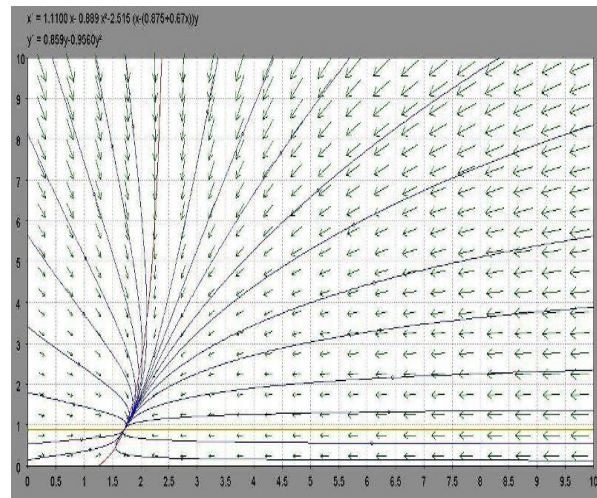
Phase Plane Figure(3)



Phase Plane Figure(4)



Phase Plane Figure(5)



Phase Plane Figure(6)

**6. Conclusions:** The Ammensal–Enemy Species are greatly influenced by the change in the value of  $g$ . Initially, the Enemy Species will have the upper hand over the Ammenal Species throughout the course of some period of time. However, after some point in time, the Ammenal Species will have the upper hand. While this was going on, the dominance reversal time happened twice, once at  $t_1^*$  and once at  $t_2^*$ . In this part of the expression,  $t_1^*$  goes down over time while  $t_2^*$  goes up.

**Overall Conclusions in a tabular form:**

Change in the Parameter	Dominance Time	Nature
$g$ increases	$t_1^*$ decreases $t_2^*$ increases	Nature of Dominance is reversed

## 7. References

[1].KapurJ.N.,MathematicalModelling, Wiley Eser,1985.

- [2].K.V.L.N.Acharyulu and N.Ch. PattabhiRamacharyulu;An Ammensal-Enemy Specie Pair With Limited And Unlimited Resources Respectively-A Numerical Approach, Int. J. Open Problems Compt. Math (IJOPCM), Vol. 3, No. 1, March 2010,73-91.
- [3].K.V.L.N.Acharyulu and N.Ch. PattabhiRamacharyulu; An Enemy-Ammensal Species Pair With Limited Resources –A Numerical Study, Int. J. Open Problems Compt. Math (IJOPCM), Vol. 3, No. 3, September 2010,339-356,
- [4].K.V.L.N.Acharyulu and N.Ch. PattabhiRamacharyulu; Mortal Ammensal and an Enemy Ecological Model with Immigration for Ammensal Species at a Constant Rate, International Journal of Bio-Science and Bio-Technology, Vol. 3, No.1, Marc 2011,39-48,
- [5].K.V.L.N.Acharyulu and N.Ch. PattabhiRamacharyulu;An Immigrated Ecological Ammensalism with Limited Resources”-International Journal of Advanced Science and Technology, Vol. 27 ,2011, 87-92.
- [6].K.V.L.N.Acharyulu and N.Ch.PattabhiRamacharyulu; A Numerical Study on an Ammensal -Enemy Species Pair with Unlimited Resources and Mortality Rate for Enemy Species”-International Journal of Advanced Science & Technology,Vol.30, May 2011,13-24.
- [7].K.V.L.N.Acharyulu and N.Ch. PattabhiRamacharyulu; An Ecological Ammensalism with Multifarious restraints-A Numerical Study” International Journal of Bio-Science and Bio-Technology,Vol. 3, No. 2, June 2011,1-12.
- [8].K.V.L.N.Acharyulu and N.Ch. PattabhiRamacharyulu; Multiple Constraints in Ecological Ammensalism-A Numerical Approach , Int. J. Advance. Soft Comput. Appl., Vol. 3, No. 2, July 2011,1-15.
- [9].K.V.L.N.Acharyulu and N.Ch. PattabhiRamacharyulu; On the Carrying capacity of Enemy Species, Inhibition coefficient of Ammensal Species and Dominance reversal time in An Ecological Ammensalism -A Special case study with Numerical approach, International Journalof Advanced Science and Technology, Vol. 43, June,2012,49-58.
- [10].Lotka A.J.(1925). Elements of Physical Biology, Williams and willians, Baltimore,1925.
- 11.Lakshmi Narayan K.(2005).A Mathematical study of a prey –predator Ecological Model with a partial cover for the prey and alternative food for the predator, Ph.D. Thesis, JNTU.
- [12].Meyer WJ. Concepts of mathematical modelling.McGraw-Hill; 1985.

- [13].Mesterton-Gibbons Michael. A technique for finding optimal two species harvesting policies. *EcolModell* 1996;92:235–44.
- [14].Paul Colinvaux A. *Ecology*. New York: John Wiley; 1986.
- [15].Phanikumar N. SeshagiriRao. N &PattabhiRamacharyulu N.Ch.,On the stability of a host - A flourishing commensal species pair with limited resources”. *Internationaljournal of logic based intelligent systems*,3(1),2009,pp. 45-54.
- [16].PhanikumarN.,Pattabhiramacharyulu N.Ch.,A three species eco-system consisting of a prey predator and host commensal to the prey” *International journal of open problems compt.math*, 3(1),2010,pp.92-113.
- [17].Srinivas NC. Some mathematical aspects of modelling in biomedical sciences. Ph.D.thesis. Kakatiya University; 1991.
- [18].Volterra V. Leconssen *LaTheorie Mathematique De La LeittePou Lavie*. Paris: Gouthier-Villars; 1931.